1. The presentation is a summary from a manuscript currently (June 2016) in review with Remote Sensing of Environment (Elsevier).

Title of submission: A functional regression model for inventories supported by aerial laser scanner data or photogrammetric point clouds

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FRA context:

Inventories supported by airborne laser data (ALS) or photogrammetric point clouds (PPC)

Model-assisted and model-based estimators

Note: extensions to hyperspectral data is also possible.
Besides the above rationale one can also argue for FRA on grounds of ‘interpretability’ and for research into how ALS and AP data connects to our plot data of a study variable.
Note: the key to success with FRA is to define the yet-to-be-explained ‘t’. It will become clear momentarily.
Note: For study variables such as volume per ha, basal area and other attributes related to size and site occupancy of trees the above assumptions appears reasonable.

The estimation ‘trick’ is to optimize the fit to first-order differences in \( X(t) \). Here we only consider first-order differences, but in other applications we could apply FRA with second-order differences, third-order differences, or a mix of these, all depending on context.
A case study from Baden-Württemberg

Rastatt state forest in the Northern Black Forest with an area of 1012 ha

456 field plots located on a 100 m × 200 m grid and stratified to coniferous (251), deciduous (36), and mixed-wood (169).

Tree attributes such as species, stem diameter (DBH), and height were collected in each sample plot. DBH was measured on a set of four nested (concentric) circular plots.

Volume (aboveground for all parts with a minimum diameter of 7 cm) was calculated by means of volume models developed for the National Forest inventory, based on taper models (Kublin et al. 2013).

Only trees located inside the forest were measured, and plot areas refer to the area inside the forest.

Note: the submitted manuscript has additional case studies from France and Norway.
Auxiliary variables (X)

- The auxiliary variables X were relative frequency counts of binned canopy heights obtained from aerial photographs (AP) and ALS first returns.

- PPC data came from the aerial photographs acquired with a Vexcel UltraCamXp camera with a focal length of 100.5 mm. The images overlapped by 80% along tracks and 60% across tracks. The ground resolution of the images was 10 cm and the extracted point cloud was interpolated to a regular raster with 1 m² resolution.

- ALS data were acquired with a Riegel LMS-Q780 laser scanner at a flying altitude of approximately 600 m above ground. The pulse repetition frequency of 400 kHz and a scan frequency of 150 Hz resulted in a ground point density of approximately 25-50 m².

- Frequency counts of ALS and AP canopy heights were binned to $T = 24$ 2.0 m wide classes for AP while the ALS data were binned to $T = 63$ 0.75 m wide classes.
Estimated regression coefficients

Note: similarity across X data sources (ALS and PPC), slight differences across strata (HW = hardwoods, MX = mixed woods, SW = softwoods).
Note the apparent divergence of the underlying height-volume relationship in the MX stratum (suggesting a need for models with a change-point). Note also the ‘typical’ increase in residual variance with increasing predictions. In model-based inference this suggest a need for a variance function for the inference about the variance of a population estimate of the mean. In a design-based inference, the variance of residuals ‘integrates’ this trend.
Conclusions

- Fit statistics with FRA are comparable to those obtained with selected LiDAR/PPC metrics
- Results are interpretable.
- The model is a true working model and affords model-assisted estimators.
- FRA is less sensitive to plot-size, location errors, and point densities.
- Comparisons across studies are feasible.
- Easy to summarize X for a large area.
- With good DEMs the X from PPC and ALS are equally suitable in forest inventories.

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Key references:
